DATA VISUALIZATION Introduction

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https://tobias.isenberg.cc/

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CONTACT PREFERENCE: e-mail



INSTRUCTOR – Tutorials

Natkamon TOVANICH

natkamon.tovanich@inria.fr



contact the TA for any questions about the tutorials and assignments **primary contact:** via e-mail

COURSE INFO https://tobias.isenberg.cc/visualization/

< 81 km/b

200 km/



understand it both at a global level and at a smaller scale, and to make decisions based on the data. Visualization turns data into visual representations that allow users to understand it and to provide them with interactive tools that are designed to efficiently navigate and analyze these representations. The class introduces students to the field of visualization, discusses various types of visualizations according to the type of data being analyzed (tabular data, hierarchical data, graphs, texts, 3D data), and teaches the process to build data analysis tools.

Administrative information:

evaluation type: multiple choice exam plus regular assignments

Instructors:

HomePage

Slides

Tutorial 1

Tutorial 2 Tutorial 3

Tutorial 4

Tutorial 5

Tutorial 6

Tutorial 7

Tutorial 8

Assignment 0

Assignment 1

Assignment 2 Assignment 3

Class Overview

- Dr. Tobias Isenberg (lectures)
- Jiayi Hong 洪佳怡 (tutorials)
- <u>Natkamon Tovanich</u> (tutorials)

Course materials:

material on these pages

- class overview
- slides (after the lectures)
- tutorial information
- assignment details
- contact information

COURSE INFO https://tobias.isenberg.cc/visualization/

- 1. General class overview Introduction to information visualization
- 2. Perception and color
- 3. Multi-dimensional data visualization
- 4. Graphs and trees
- 5. Time-dependent data
- 6. Storytelling with data
- 7. Interaction

RECOMMENDED READINGS



 \rightarrow links to the books on the class website

GRADING SCHEME

- Written multiple-choice exam: 50%
- Assignments/project: 50%
 More information later, after the break

Introduction to Human-Computer Interaction

 \leftarrow Encode your student number

- Time period: 8:00 11:00
- Duration of the exam: 180 min
- Number of pages: 8
- Materials allowed: Pencils, erasers

Please write your answers directly on the exam paper.

_								nere, and write the student number
0	0	0	0	0	0	0	0	again as well as your given name and
1	1	1	1	1	1	1	1	family name below. If you cannot re-
2	$\Box 2$	2	$\square 2$	2	$\square 2$	2	2	number X you see at the top of the
3	3	3	3	3	3	3	3	exam sheet in this code $+X/Y/Z+$.
4	4	4	4	4	4	4	4	Student number:
5	5	5	5			5	5	
6	6	6	6	6	6	6	6	Cirron name:
7	7	7	7	7	7	7	7	Given name.
8	8	8	8	8	8	8	8	
9	9	9	9	9	9	9	9	Family name:

- The questions with the symbol \clubsuit can have none, one, or more than one possible correct answers. All other questions have exactly one correct answer.
- Please answer the questions like this: \boxtimes ; use a **pencil** (hardness HB), and make clear marks. To correct, clearly erase the wrong mark and put a new one (if needed). If you cannot erase because you did not bring a pencil, make the incorrect box completely black.
- All multiple-choice questions are worth one point. For it to be counted as answered correctly, all correct answers and no incorrect answer have to be selected.
- Do not fold the answer sheet(s), do not write on the back.

Question 1 Student did NOT bring a pencil. Do NOT fill out yourself.

Student brought a pencil.

Student did not bring a pencil.

Multiple-Choice Questions:

 $\label{eq:Question 2} \qquad \text{Driving to the supermarket but ending up at work is an example of which type of error}$

description error a mistake capture error none of the above mode error

Tutorials

https://tobias.isenberg.cc/visualization/

- 1. Data wrangling with OpenRefine
- 2. Working with Tableau
- 3. Data vis with Altair # 1: Basics
- 4. Data vis with Altair # 2: Exercise
- 5. Data vis with Altair # 3: Interaction & selection
- 6. Data apps with Streamlit
- 7. Streamlit continued, Data dashboards with Panel or Cartographic Visualization in Altair

Prepare for Tutorial

	Tutorials / Tutorial 1	Print Search: Go
HomePage		
	Tutorial: Data Cleaning with Ope	nRefine
Class Organization	Teacher: Natkamon Tovanich	
Class Overview Slides Recommended Readings Grading and Rules	In this tutorial, you will learn to use Google Refine to analysis. We will perform some cleaning together in c	clean a dataset and create files for class.
Links and References	Getting Started	
Labs/Assignments	Install Google Refine You can download and in	stall it from here
Tutorials Schedule <u>OpenRefine</u> Tableau Altair	 You should install the "OpenRefine 3.7.7" at the version). Download the following dataset: <u>UniversityData</u> 	e top of the page (not the beta a.csv
Panel Observable	References	
Assignments Overview Team Formation	 The Open Refine documentation is available <u>he</u> Here is the pointer to <u>the Open Refine Express</u> 	<u>ere</u> . ion Language.
Exploratory Data Analysis Interactive Data Storytelling	Reminder	
	Next week's tutorial will introduce <u>Tableau</u> . Please ins request a free student license here.	stall Tableau in advance. You could

Prepare for EACH Tutorial

Install Tableau and register for the student license

PRICING SIGN IN

FREE STUDENT LICENSE

‡‡‡ + a b | e a u.

Why Tableau V Products V Solutions V Resources V Partners V



We offer free one-year Tableau licenses to students at accredited academic institutions through our Tableau for Students program. Receive access to our entire eLearning suite once verified.

Assignments

https://tobias.isenberg.cc/visualization/

- two major assignments for the class
- detailed instructions on the class website
- assignment results count for 50% of the final grade
- work in groups of 2 students (= Assignment 0)
- find a group and let us know about groups
 before the third class (deadline: 23:00 on day before)
- strict deadlines; point deduction if late

Assignment 1

https://tobias.isenberg.cc/visualization/

Data Proposals and Exploratory Data Analysis (30 points)

Part 1 (group work)

- pick a topic area of interest
- find a dataset that can provide insights into that topic
- describe the dataset

Part 2 (individual work)

- each team member should find a research question about the dataset
- produce one exploratory visualization that effectively answers that research question
- each team member must pick different questions
- write up on findings you gain

Assignment 2

https://tobias.isenberg.cc/visualization/

Create an interactive data storytelling (70 points)

- at least 3 different views/visualization components
- multiple views coordinated with linked highlighting
- at least 2 UI widgets allow users to filter the data or update certain views interactively
- interactive tooltips are shown when users hover over marks, at least in one view

You are free to use libraries introduced in the class or any code-based libraries. However, you are not allowed to use dashboard software for the final project.

- online tool
- code base
- video presentation
- presentation slide

Schedule

week 1	week 2	week 3	week 4	week 5	week 6	week 7	week 8	week 9	week 11	final deadline
Jan. 23	Jan. 30	Feb. 6	Feb. 13	Feb. 20	Feb. 27	Mar. 6	Mar. 13	Mar. 20	Mar. 27	Mar. 31
L1	L3	T1	break	break	T3	L5	L6	L7	exam	_
L2	L4	T2	break	break	T4	Τ5	T6	T7	exam	_
start A0		start A1			start A2					
		A0 due Feb. 5, 23:00 CET			A1 due Feb. 26, 23:00 CET					A2 due 23:00 CET

ANY QUESTIONS?

- please ask questions during the lecture
 - if I speak too fast
 - if I use terms or expressions that you do not understand
 - if you do not understand a concept
 - there are no dumb questions!
 - there is no impact on the grade!
- e-mail us if you have questions in-between lectures

FINAL NOTE BEFORE WE START

• we are always looking for good students with visualization background for internships/MSc theses and, later PhD theses – contact us if interested



Why
VISUALIZE DATA?

AFTER TODAY YOU WILL...

have gained an overview of visualization basics

learned basic principles of data representation and interaction

understand data types, marks, visual variables

DATA EXPLORATION / INSIGHT

confirmatory analysis

- start with a hypothesis about the data
- confirm that it is true

exploratory analysis

- likely no a-priori information about the data
- not sure about patterns and information present
- explore to create hypotheses & confirm later

focus of fully automated analysis methods

focus of visualization

DATA EXPLORATION / INSIGHT

Often with expert / complex tools



POLARIS

Either for any data (here data tables)

Taxi Trajectories for Selecting Billboard Locations

Dongyu Liu, Di Weng, Yuhong Li, Jie Bao, Yu Zheng, Huamin Qu, and Yingcai Wu



Or for dedicated data / tasks

PERSUATION, EDUCATION, MOTIVATION







 \rightarrow personal information and motivation

BIG RESEARCH QUESTIONS IN VISUALIZATION

how can humans effectively access data?

- understand its structure?
- make comparisons?
- make decisions?
- gain new knowledge?
- convince others?





EXAMPLE

						IV	
х	у	х	у	х	у	х	у
10.0	8.04	10.0	9.14	10.0	7.46	8.0	6.58
8.0	6.95	8.0	8.14	8.0	6.77	8.0	5.76
13.0	7.58	13.0	8.74	13.0	12.74	8.0	7.71
9.0	8.81	9.0	8.77	9.0	7.11	8.0	8.84
11.0	8.33	11.0	9.26	11.0	7.81	8.0	8.47
14.0	9.96	14.0	8.10	14.0	8.84	8.0	7.04
6.0	7.24	6.0	6.13	6.0	6.08	8.0	5.25
4.0	4.26	4.0	3.10	4.0	5.39	19.0	12.50
12.0	10.84	12.0	9.13	12.0	8.15	8.0	5.56
7.0	4.82	7.0	7.26	7.0	6.42	8.0	7.91
5.0	5.68	5.0	4.74	5.0	5.73	8.0	6.89

Raw Data from Anscombe's Quartet

STATISTICAL ANALYSIS

For all four columns, the statistics are identical

	I	I	I	I	II	IV	
х	у	х	у	х	у	х	у
10.0	8.04	10.0	9.14	10.0	7.46	8.0	6.58
8.0	6.95	8.0	8.14	8.0	6.77	8.0	5.76
13.0	7.58	13.0	8.74	13.0	12.74	8.0	7.71
9.0	8.81	9.0	8.77	9.0	7.11	8.0	8.84
11.0	8.33	11.0	9.26	11.0	7.81	8.0	8.47
14.0	9.96	14.0	8.10	14.0	8.84	8.0	7.04
6.0	7.24	6.0	6.13	6.0	6.08	8.0	5.25
4.0	4.26	4.0	3.10	4.0	5.39	19.0	12.50
12.0	10.84	12.0	9.13	12.0	8.15	8.0	5.56
7.0	4.82	7.0	7.26	7.0	6.42	8.0	7.91
5.0	5.68	5.0	4.74	5.0	5.73	8.0	6.89

Mean of <i>x</i>	9.0
Variance of <i>x</i>	11.0
Mean of <i>y</i>	7.5
Variance of <i>y</i>	4.12
Correlation between x and y	0.816
Linear regression line	<i>y</i> = 3 + 0.5 <i>x</i>

VISUAL REPRESENTATION OF THE DATA

Visual representation reveals a different story

•	10 -	IV		II	I	I	I	I	I.	
•	7 8-	у	х	у	х	у	х	у	Х	
	6-	6.58	8.0	7.46	10.0	9.14	10.0	8.04	10.0	
		5.76	8.0	6.77	8.0	8.14	8.0	6.95	3.0	
		7.71	8.0	12.74	13.0	8.74	13.0	7.58	3.0	
4 6 8 10 12 14 16 18 v1		8.84	8.0	7.11	9.0	8.77	9.0	8.81	0.0	
		8.47	8.0	7.81	11.0	9.26	11.0	8.33	1.0	
	Г	7.04	8.0	8.84	14.0	8.10	14.0	9.96	4.0	
•	12 -	5.25	8.0	6.08	6.0	6.13	6.0	7.24	.0	
	10 -	12.50	19.0	5.39	4.0	3.10	4.0	4.26	4.0	
	-8 X	5.56	8.0	8.15	12.0	9.13	12.0	10.84	12.0	
	6 -	7.91	8.0	6.42	7.0	7.26	7.0	4.82	7.0	
	4 -	6.89	8.0	5.73	5.0	4.74	5.0	5.68	5.0	

хЗ



12



χ	Mean	:	54.0236753
Y	Mean	:	48.0970794
χ	SD	:	14.5298540
Y	SD	:	24.7943127
Сс	orr.	:	+0.3280926





https://www.autodeskresearch.com/publications/samestats

Why visual data representations?

- Vision is our most dominant sense
- We are very good at recognizing visual patterns
- We need to see and understand in order to explain, reason, and make decisions



all examples from: http://vis.stanford.edu/protovis/

Other benefits of visualization

- expand human working memory
 - offload cognitive resources to the visual system
- reduce search
 - by representing a large amount of data in a small space
- enhance the recognition of patterns
 - by making them visually explicit
- aid monitoring of a large number of potential events
- provides a manipulable medium & allows exploration of a space of parameter values







Visualization

- Create visual representation
- Includes interaction

Official Definition:

The use of computer-supported, interactive, visual representations of data to amplify cognition. [Card et al., 1999]

READINGS IN INFORMATION VISUALIZATION USING VISION TO THINK MANMENERENDON STOART & CARD JOCK D. MANKANIAN BEN SINKEDREAM



Functions of Visualizations

- recording information
 - Tables, blueprints, satellite images
- processing information
 - needs feedback and interaction
- presenting information
 - share, collaborate, revise
 - for oneself, for one's peers, and to teach
- seeing the unseen





The New York Times


HISTORICAL EXAMPLES

Visualization of data has been practiced for hundreds of years...

VERY EARLY EXAMPLES



5500 BC – Mesopotamian Clay Tokens

tokens that externalize information, support visual thinking, and enhance cognition way before paper and writing were invented



2600 BC – Quipus

assemblies of knotted ropes that were used in South America as a data storage; color, relative position of knots, knot types, and rope length were used to encode categorical and quantitative variables



500 BC - Pebble Voting

the earliest participatory visualizations were probably voting systems

THE BROADWAY STREET PUMP

- In 1854 cholera broke out in London
 - 127 people near Broad Street died within 3 days
 - 616 people died within 30 days
- "Miasma in the atmosphere"
- Dr. John Snow was the first to link contaminated water to the outbreak of cholera
- How did he do it?
 - he talked to local residents
 - identified a water pump as a likely source
 - used maps to illustrate his theory
 - convinced authorities to disable the pump





JOHN SNOW, 1854



Replica memorial of the Broadway street pump Creative commons CC-BY-SA 4.0 by Wikipedia author Jamzze

NAPOLEON'S MARCH ON MOSCOW

Named the best statistical graphic ever drawn (by Edward Tufte)

- Includes: spatial layout linked with stats on: army size, temperature, time
- Tells a story in one overview



Charles Minard, 1869

More info: The Visual Display of Quantitative Information (Tufte)



https://thoughtbot.com/blog/analyzing-minards-visualization-of-napoleons-1812-march

Temperature During The Retreat



https://thoughtbot.com/blog/analyzing-minards-visualization-of-napoleons-1812-march





TODAY

Visualizations are done by many people...

The New York Eimes

Districts Across the Country Shift to the Right





Professionals (journalists, analysts, ...)

TheUpshot

Where Have All the Houses Gone?

The inventory of homes for sale is startlingly low. The pandemic is part of the reason, but it's not the whole story.





Published Feb. 26, 2021 Updated March 2, 2021

The number of homes for sale nationally has plummeted









Project Ukko - Seasonal Wind Predictions for the Energy Sector

Weather forecasts predict future wind conditions only in the range of weeks. Climate predictions look at big changes over years and decades. However, for energy traders, wind farm managers and...

Enthusiasts, freelancer, ...

Markus Hoffmann, Hannah Kleine-Weber, Simon Schroeder, Nadine Krüger, Tanja Herrler, Sandra Erichsen, Tobias S. Schiergens, Georg Herrler, Nai-Huei Wu, Andreas Nitsche, Marcel A. Müller, Christian Drosten, Stefan Pöhlmann, SARS-CoV-2 Cell Entry Depends on ACE2 and TMPRSS2 and Is Blocked by a Clinically Proven Protease Inhibitor, Cell, Volume 181, Issue 2, 2020,



в





THE WORLD CUP'S BIG GUNS

% OF TEAM'S RUNS SCORED BY TOP SCORER





People who shouldn't

RESOURCES

- Visualization conferences
 - ieeevis.org
- Blogs
 - <u>http://eagereyes.org/</u>
 - <u>http://flowingdata.com/</u>
 - <u>http://www.informationisbeautiful.net/</u>
 - https://www.visualisingdata.com/blog/
 - <u>https://pudding.cool/</u>
 - <u>https://junkcharts.typepad.com/</u>
 - <u>https://badvisualisations.tumblr.com/</u>

- Books
 - Textbooks
 - Readings in Information Visualization: Using Vision to Think (a bit old now but good intro)
 - Information Visualization (Robert Spence a light intro, I recommend as a start)
 - Information Visualization Perception for Design (Colin Ware, focused on perception and cognition)
 - Interactive Data Visualization: Foundations, Techniques, and Applications (Ward et al.)
 - Visualization Analysis and Design (Tamara Munzner, most recent book)
 - Examples
 - Beautiful Data (McCandless)
 - Now You See it (Few)
 - Tufte Books: Visual Display of Quantitative Information (and others)
 - ... (many more, ask me for details)

It is difficult to create





HOW DO WE ARRIVE AT A VISUALIZATION?



The Visualization Pipeline

From [Spence, 2000]

HOW DO WE ARRIVE AT A VISUALIZATION?



PITFALLS

- Selecting the wrong data
- Selecting the wrong data structure
- Filtering out important data
- Failed understanding of the types of things that need to be shown
- Choosing the wrong representation
- Choosing the wrong presentation format
- Inappropriate interactions provided to explore the data

RECAP

- So far you
 - learned what visualization is
 - learned about the advantages of visualization
 - saw a number of examples (historical and new)
- Next
 - you will get to know your data
 - you will learn about the basic components of visualization

DATA

- Data is the foundation of any visualization
- The visualization designer needs to understand
 - the data properties
 - know what meta-data is available
 - know what people want from the data

DATA SET AND ATTRIBUTE TYPES

(some of them, more later & even more in the cited literature)

TABLES



Example:

Items: drinks Attributes: color, calories, name, ...

NETWORKS



Example:

Item = nodes: people Item = links: co-authorship

Node attributes: name, experience, ... Link attributes: #of papers

GEOMETRY (SPATIAL)

Specifies information about the shape of items with explicit spatial position



Item = countries Positions = location on the planet



Figure 2.4. The detailed structure of the four basic dataset types.

ATTRIBUTE TYPES

- Nominal (sometimes called categorical) 🍎 🌢 🍐 🛩
 - Fruits: apples, oranges
 - Can be compared =, \neq
- Ordered
 - Ordinal
 - T-shirt sizes: S, M, L, XL
 - Can be compared & ordered, but **not** calculated with: =, \neq , <, >
 - Quantitative
 - Counts and amounts, 5kg / 10kg
 - you can do =, ≠, <, >, , +, ×, ÷



WHY IS THIS IMPORTANT?

- Nominal, ordinal, and quantitative data are best expressed in different ways visually
- Data types often have inherent tasks
 - geometry (understand spatial relationships)
 - trees (understand parent-child relationships)





• But:

- any data type (1D, 2D, ...) can be expressed in a multitude of ways!

VISUALIZATION BUILDING BLOCKS



Basic geometric element data depict items or links



POINTS

- "A point represents a location on the plane that has **no theoretical length or area**. This signification is independent of the size and character of the mark which renders it visible."
- a location
- marks that indicate points can vary in all visual variables



LINES

• "A line signifies a phenomenon on the plane which has **measurable length but no area**. This signification is independent of the width and characteristics of the mark which renders it visible."



• a boundary, a route, a connection

AREAS

- "An area signifies something on the plane that has measurable size.
 This signification applies to the entire area covered by the visible mark."
- an area can change in position but not in size, shape or orientation without making the area itself have a different meaning


which marks do you see?



which marks do you see?



which marks do you see?



VISUAL CHANNELS

Also often called visual variables



These are the most common but there are more

which visual channels encode data?





which visual channels encode data?





which visual channels encode data?



ADDITIONAL CHANNELS

motion

 direction, acceleration, speed, frequency, onset, 'personality'



• saturation

 color as Bertin uses it largely refers to hue, saturation != value



ADDITIONAL CHANNELS

• flicker

- frequency, rhythm, appearance
- depth? 'quasi' 3D
 - depth, occlusion, aerial perspective, binocular disparity
- illumination

transparency

CHARACTERISTICS OF VISUAL VARIABLES

• selective:

Can this variable allow us to spontaneously differentiate/isolate items from groups?

• associative:

Can this variable allow us to spontaneously group items in a group?

• ordered:

Can this variable allow us to spontaneously perceive an order?

• quantitative:

Is there a numerical reading obtainable from changes in this variable?

length (resolution): Across how many changes in this variable are distinctions possible?

From Semiology of Graphics (Bertin)

VISUAL VARIABLE: POSITION

- ✓ selective
 - associative
 - 🗸 order
- quantitative
- \checkmark length (resolution)







From Semiology of Graphics (Bertin)

VISUAL VARIABLE: SIZE

- selective
- associative
- 🗸 🔹 order
- 🗠 quantitative
- \checkmark length (resolution)



SIZE



points lines

areas

VISUAL VARIABLE: SHAPE



- ✓ quantitative
- length (resolution)
 infinite



SHAPE



points lines areas

VISUAL VARIABLE: VALUE



- ≠ quantitative
 - length (resolution)
 - theoretically infinite but practically limited
 - association and selection \sim < 7 and distinction \sim 10

VALUE



points lines areas

VALUE

• Ordered, cannot be reordered



Values not ordered correctly according to scale Information has to be read point by point

Values ordered correctly Image much more useful

annual deaths per 1000 inhabitants, Paris

VISUAL VARIABLE: COLOR

- selective
- associative ${}^{\bullet}$
- ordered \neq ۲



- quantitative \neq

 - length (resolution) •
 - theoretically infinite but practically limited
 - association and selection \sim < 7 and distinction \sim 10

VISUAL VARIABLE: ORIENTATION



- ✓ quantitative
 - length (resolution)
 - ~5 in 2D; ? in 3D

ORIENTATION



points lines areas

VISUAL VARIABLE: TEXTURE

selective



- associative
- ≠ ordered



≠ • quantitative



- length (resolution)
 - theoretically infinite

TEXTURE



points lines areas

VISUAL VARIABLE: MOTION

selective

- motion is one of our most powerful attention grabbers
- associative
 - moving in unison groups objects effectively
- ≠ order
- ✓ quantitative
 - subjective perception
 - length (resolution)
 - distinguishable types of motion?



VISUAL VARIABLES

Visual Variable	Selective	Associative	Quantitative	Order	Length	
Position	Yes	Yes	Yes	Yes	Dependant on resolution	
Size	Yes	Yes	Approximate	Yes	Association: 5; Distinction: 20	
Shape	With Effort	With Effort	No	No	Infinite	
Value	Yes	Yes	No	Yes	Association: 7; Distinction: 10	
Hue	Yes	Yes	No	No	Association: 7; Distinction: 10	
Orientation	Yes	Yes	No	No	4	
Grain	Yes	Yes	No	No	5	
Texture	Yes	Yes	No	No	Infinite	
Motion	Yes	Yes	No	Yes	Unknown	

HOW TO CHOOSE CHANNELS?

EXPRESSIVENESS

show **all of, and only,** the information in the attributes (nothing more, nothing less)

Example: an ordered attribute needs to look ordered, an unordered attribute should not

This mismatch is a common beginner's mistake

EXPRESSIVENESS

luminance is ordered, cannot be reordered





Values not ordered correctly according to scale Information has to be read point by point

Values ordered correctly Image much more useful

annual deaths per 1000 inhabitants, Paris

EXPRESSIVENESS

luminance is not quantitative



if Portugal is 1, what is France? you need a legend!



if Portugal is 1, what is France? still hard, but doable

HOW TO CHOOSE CHANNELS?

EFFECTIVENESS

the importance of the attribute matches the saliency of the channel:

the most important attributes should be encoded with the most effective channels





EFFECTIVENESS

Accuracy: How accurately values can be estimated?

Discriminability: How many different values can be perceived?

Separability: How much interaction there is with multiple encodings?

Popout: How easy it is to spot some values from the rest?

Grouping: How good a channel is in conveying groups?

SUMMARY

	Quantitative		Ordinal		Nominal	
More Accurate	Position		Position	•••	Position	•.•
Î	Length	=	Density		Hue	
	Angle	4	Saturation		Density	
	Slope	11	Hue		Saturation	
	Area	••	Length	=	Shape	
	Density		Angle	2	Length	=
	Saturation		Slope	11	Angle	4
↓ I	Hue		Area	••	Slope	11
Less Accurate	Shape		Shape		Area	••

Jacques Bertin, refined by Cleveland&McGill, then by Card&Mackinlay

→ Magnitude Channels: Ordered Attributes



→ Identity Channels: Categorical Attributes

Most 🕨

Effectiveness

Least



WHAT WE UNDERSTAND SO FAR



 Slope Hue ••• Area Less Accurate Shape • • • Shape • • • Area

...

...

...

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11

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