

# **Computer Graphics**

## **3D Object Representations**

# What to Specify for a 3D Shape?

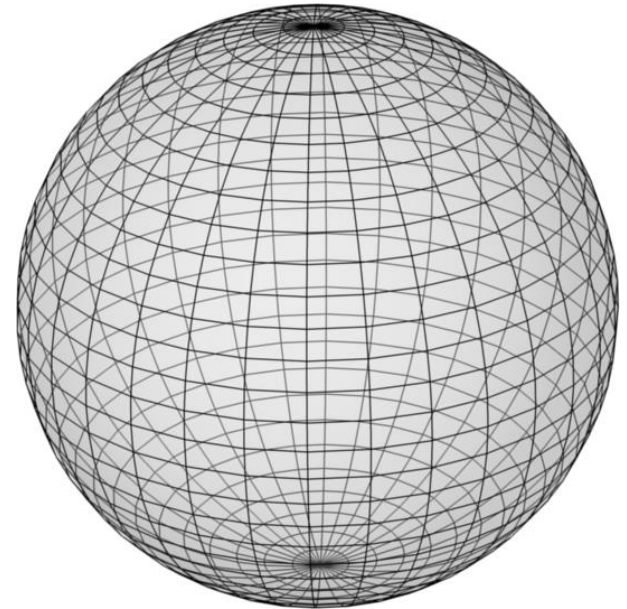
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- geometry
  - shapes, positions
  - connectivity, inside/outside
- material properties
  - visuals, textures  
(plastic, wood, metal, etc.)
  - other material properties  
(elasticity, mass, etc.)
- behaviour/animation
- more depending on the specific application

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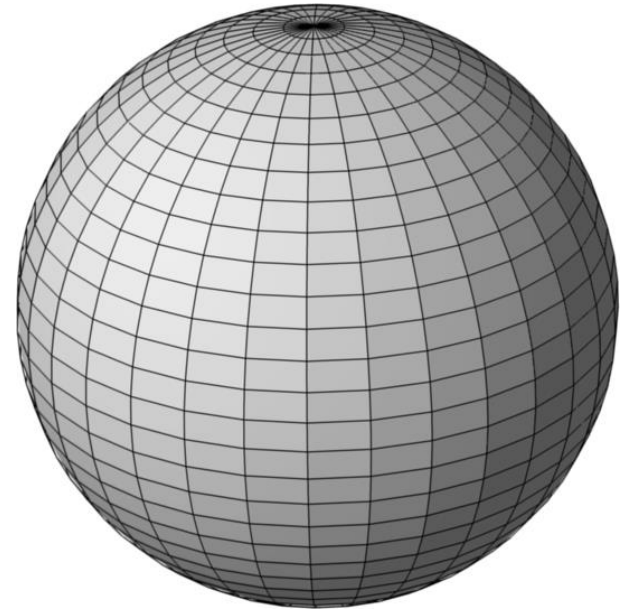
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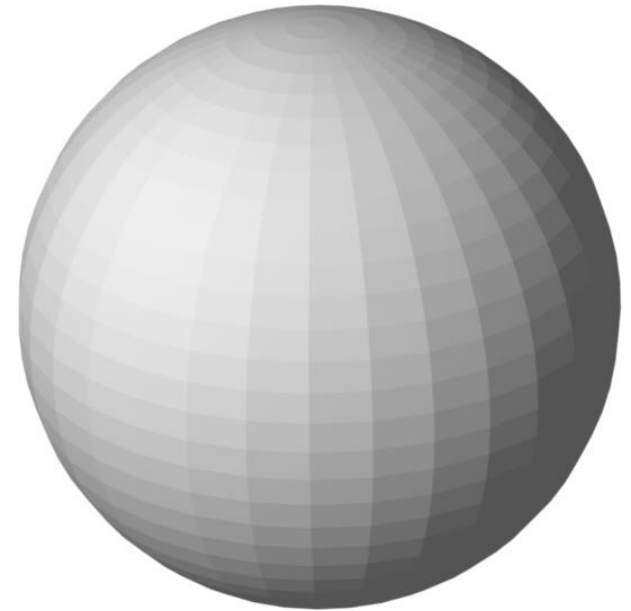
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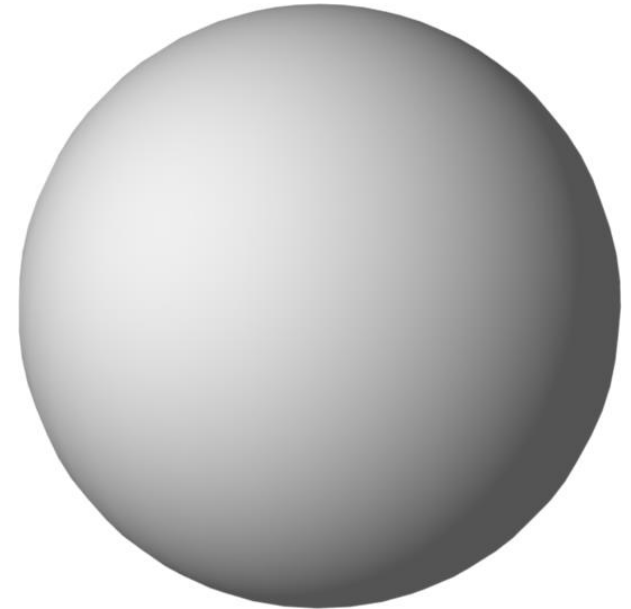
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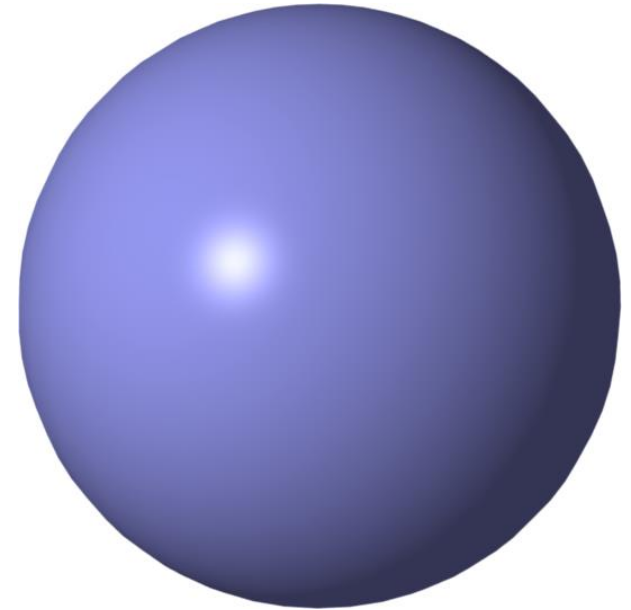
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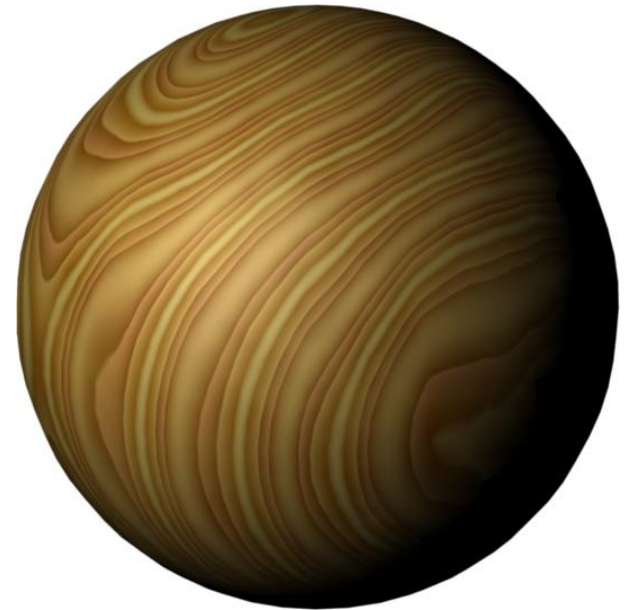
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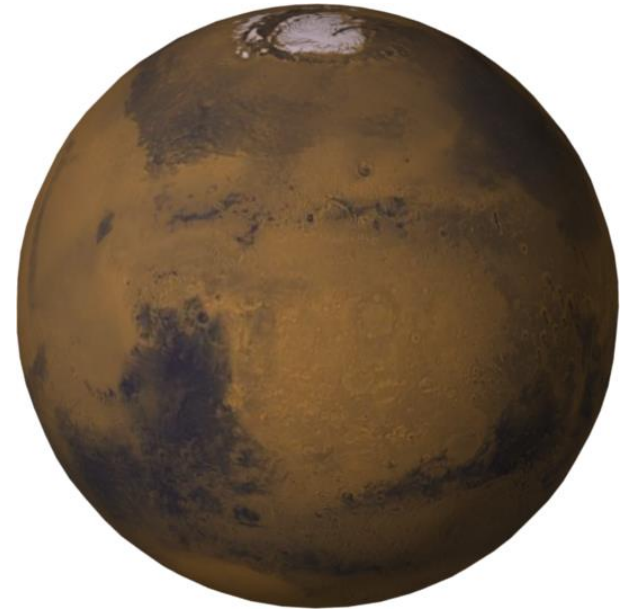




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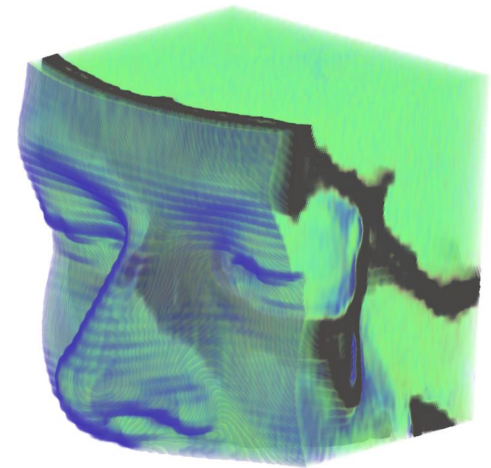
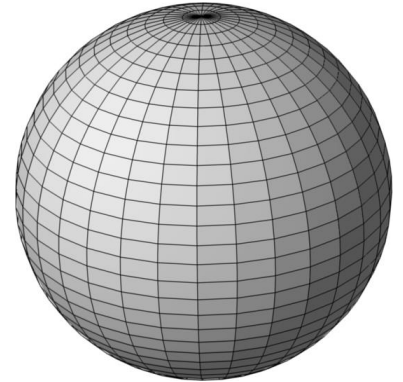
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# How to Specify a 3D Geometry?

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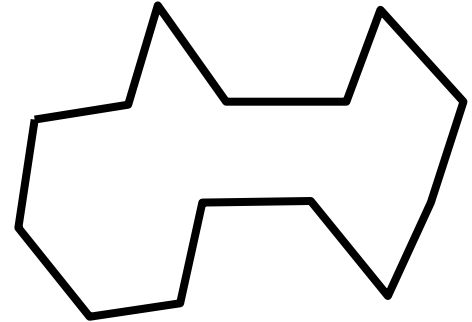
- boundary representations (b-reps)
  - meshes
  - piecewise smooth surfaces
- volume representations
  - voxel models
  - implicit surfaces
  - CSG: constructive solid geometry
  - space partitioning
    - BSP trees: binary space partitioning
    - octrees



# B-Reps: Polygonal Meshes

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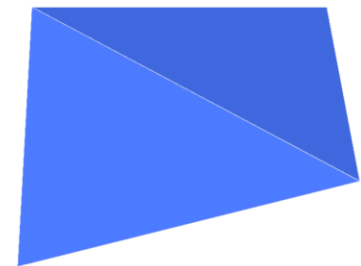
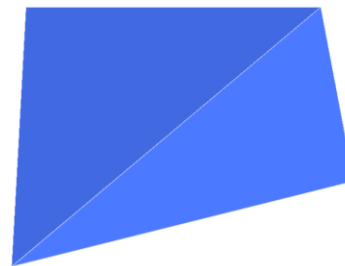
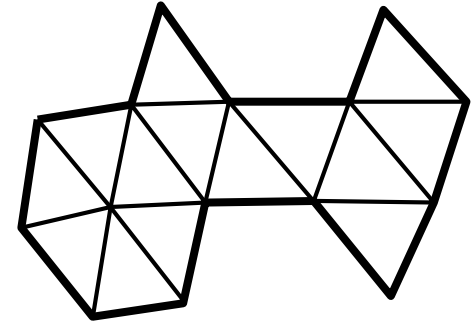
- polygons to define the surface of objects



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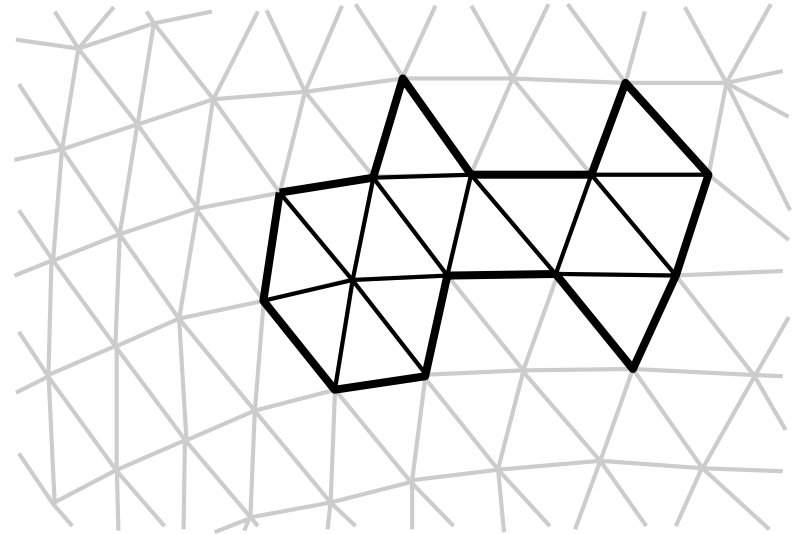
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- triangle meshes
  - polygon with fewest vertices
  - always convex & planar  
→ defines unique surface



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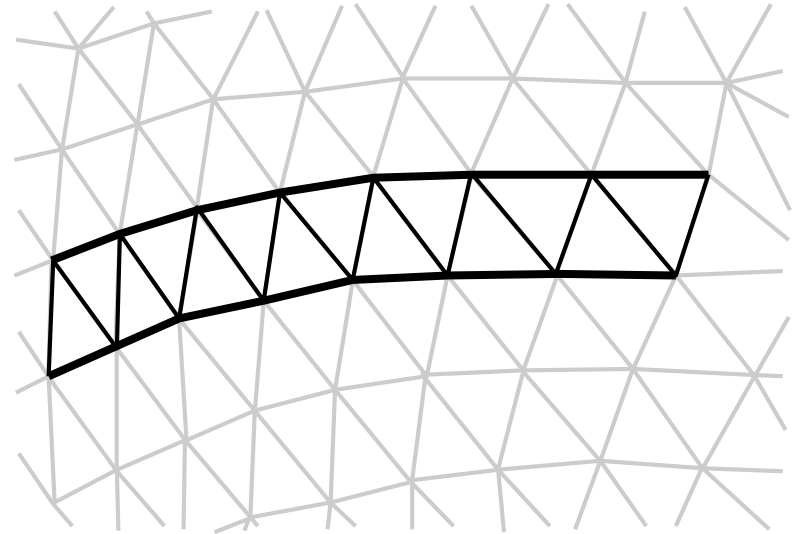
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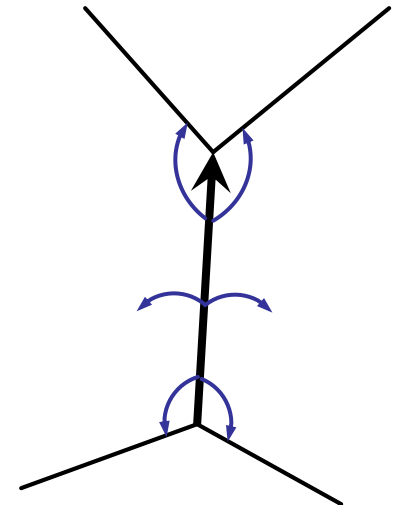
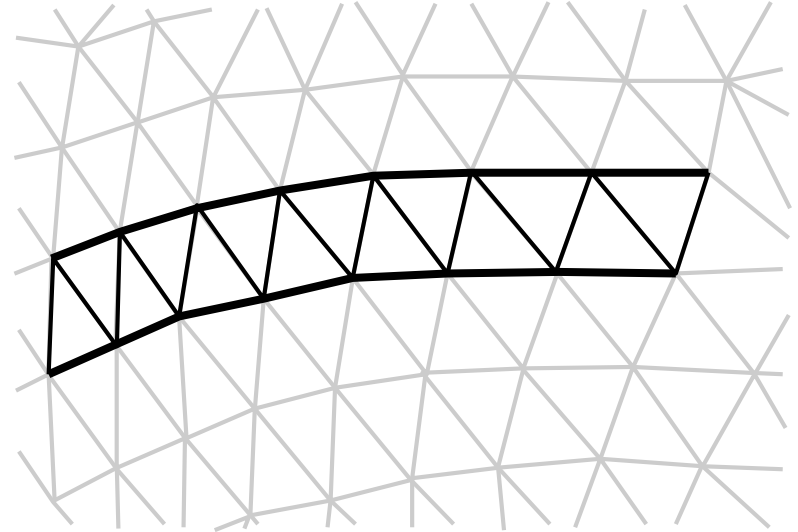
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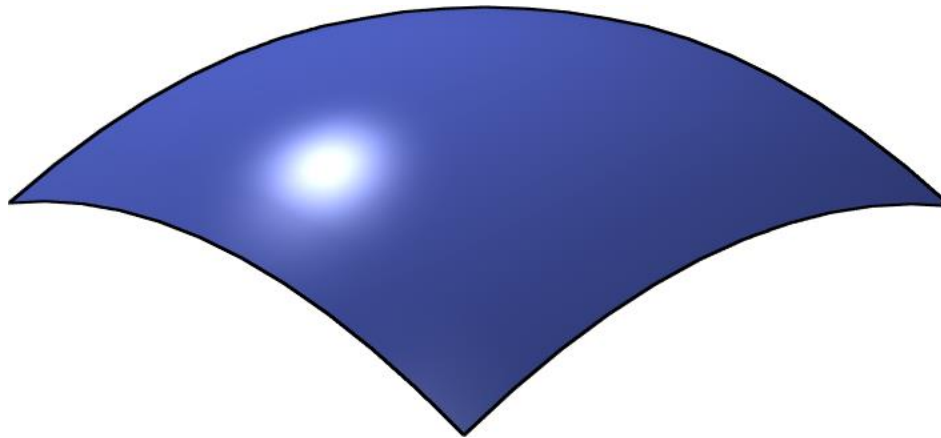
- polygons to define the surface of objects
- triangle meshes
  - polygon with fewest vertices
  - always convex & planar  
→ defines unique surface
- triangle strips: faster rendering
- more complex mesh data structures (e.g., Winged Edge)



# B-Reps: Piecewise Smooth Surfaces

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- surface constructed from patches
- patches can be curved and are smooth
- patches satisfy a continuity constraint
- e.g., Bézier, Spline, NURBS surfaces

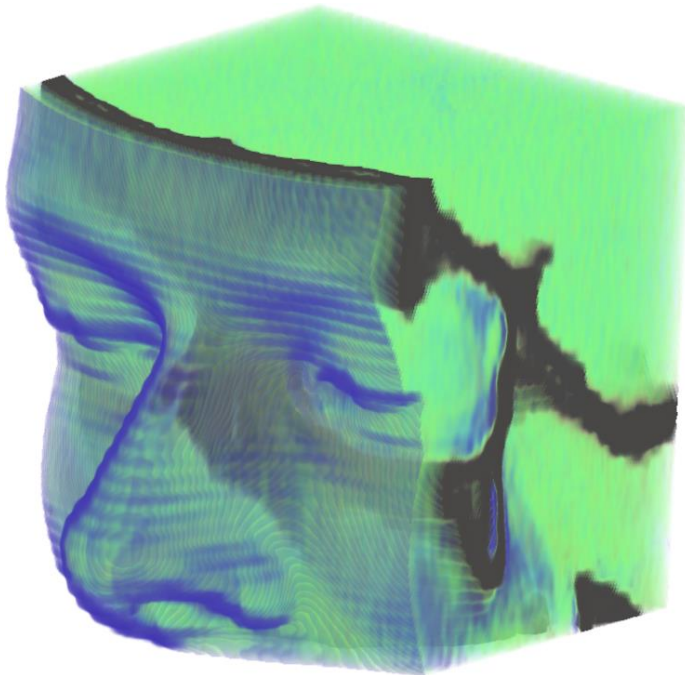




# Volumes: Voxel Models

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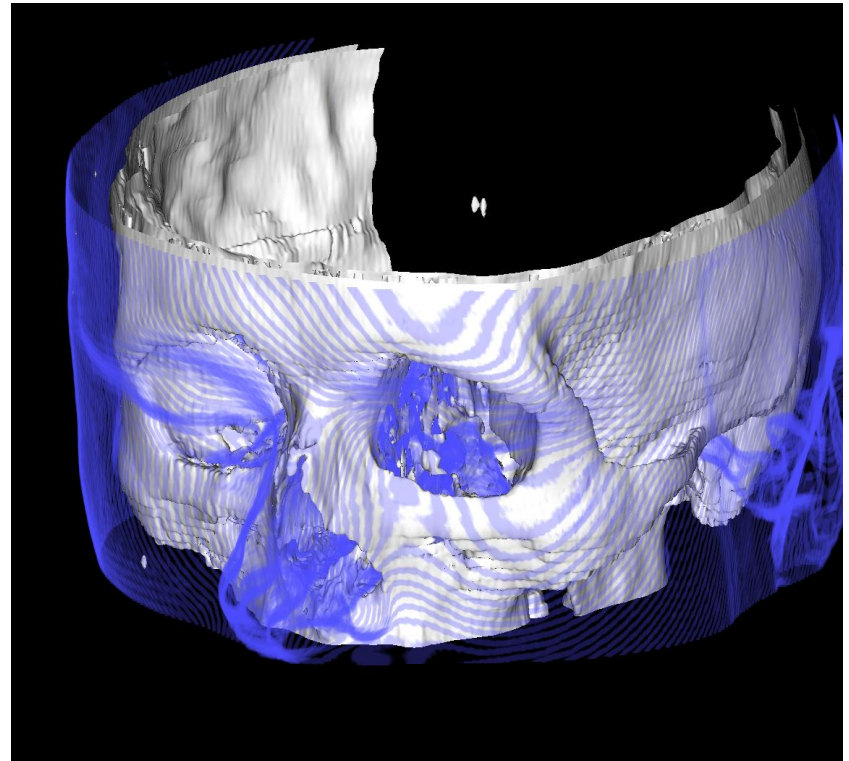
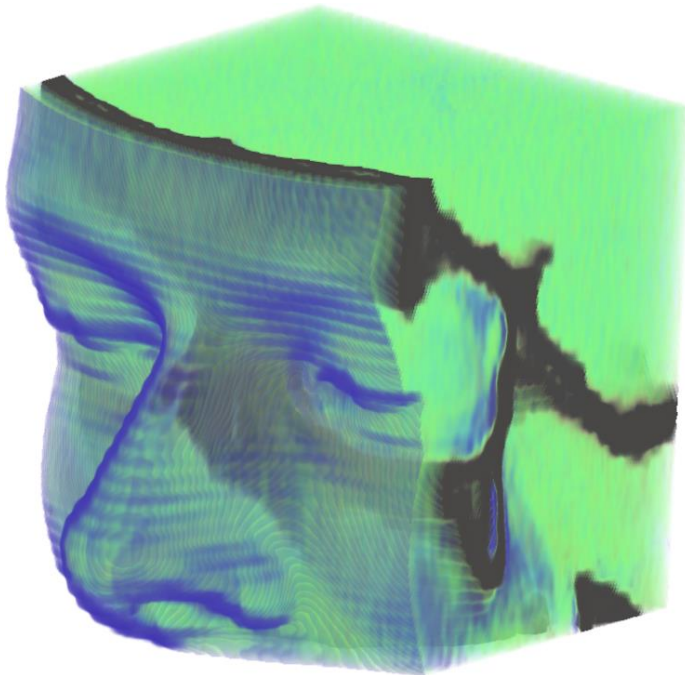
- sampling of a volume in regular intervals
- samples as cubes, or as general boxes
- several properties can be sampled



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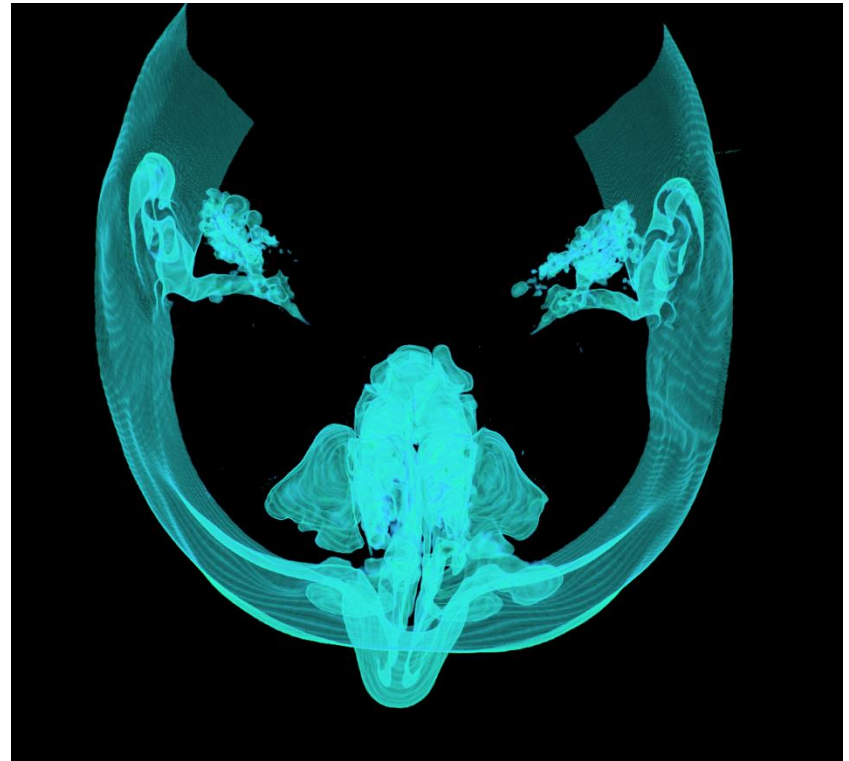
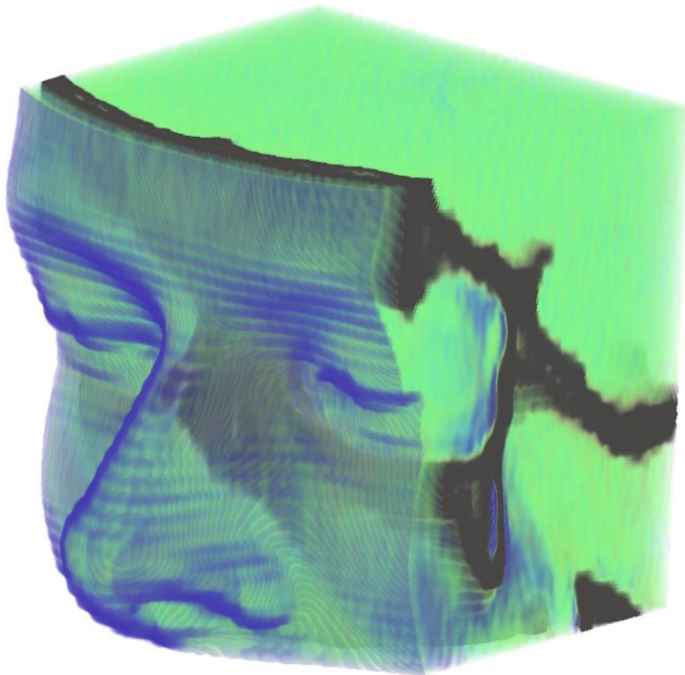
- shapes: *iso-value* to specify special level
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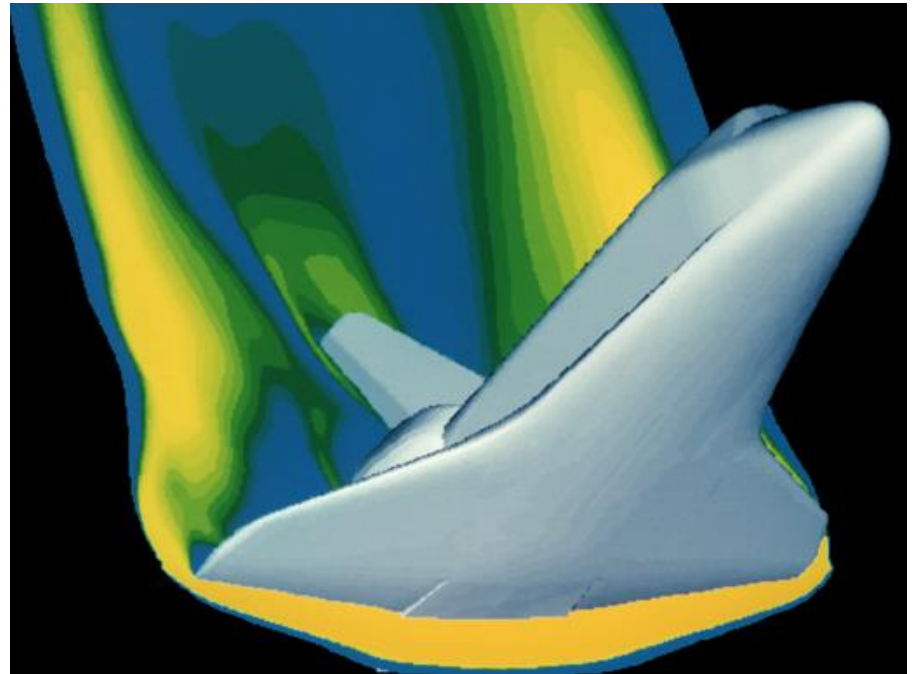
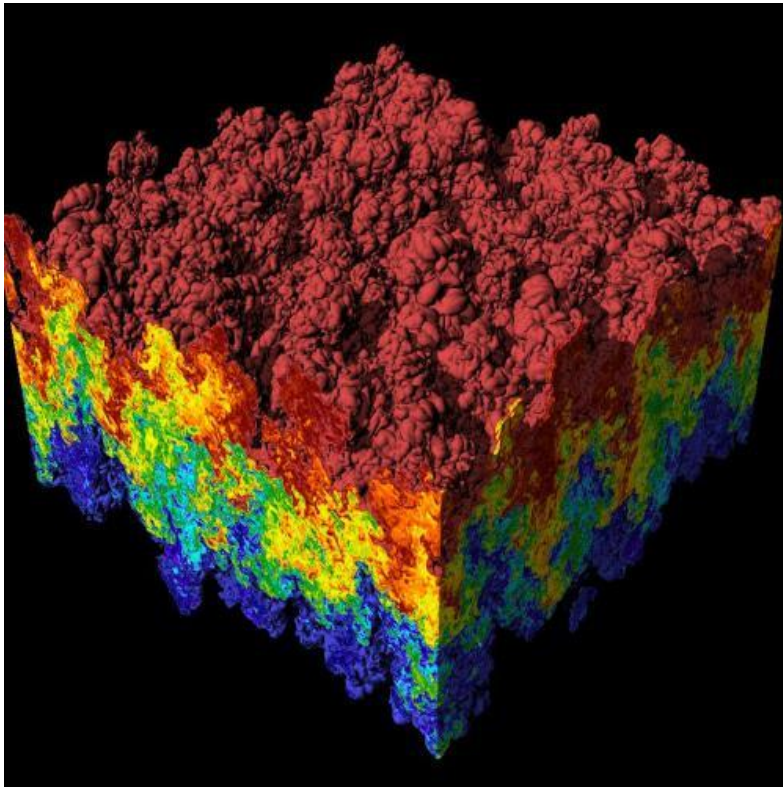




# Volumes: Voxel Models

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- heavily used in medical imaging (based on CT, MRI) and fluid dynamics etc.



# Volumes: Implicit Surfaces

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- description of shapes through implicit equations; e.g., sphere:

$$F(x, y, z) = \sqrt{x^2 + y^2 + z^2}$$

$$r = \sqrt{x^2 + y^2 + z^2}$$

$$0 = \sqrt{x^2 + y^2 + z^2} - r$$

iso-value



- iso-values defining boundary & inside
- use: mathematics, chemistry, hq rendering

# Volumes: Implicit Surfaces

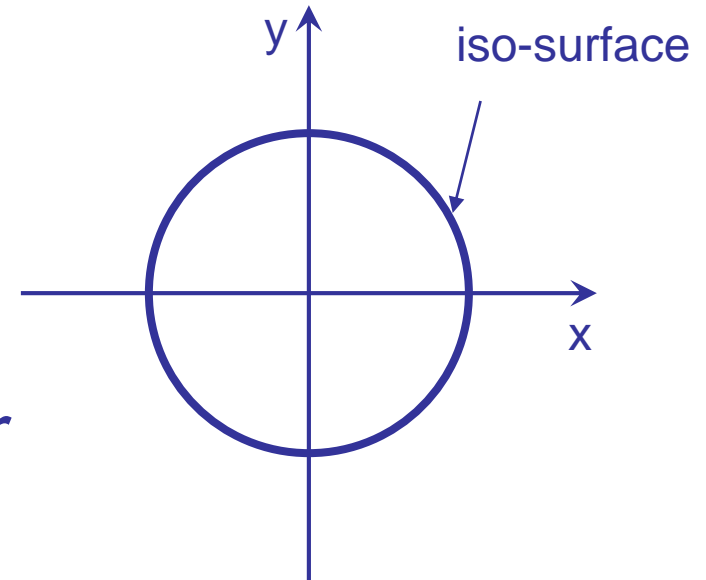
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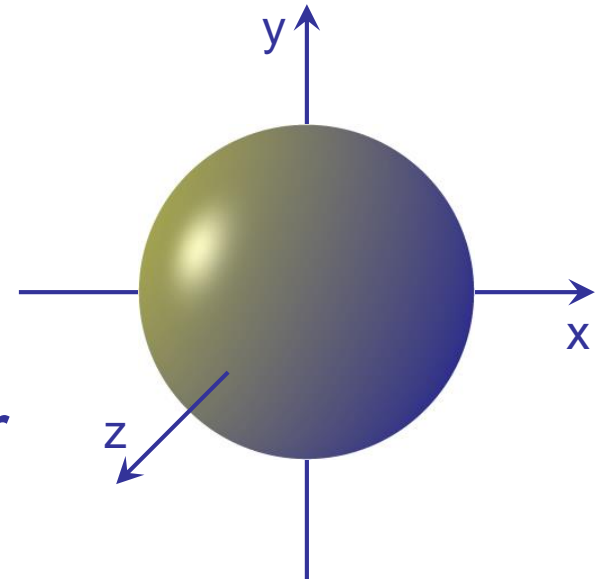
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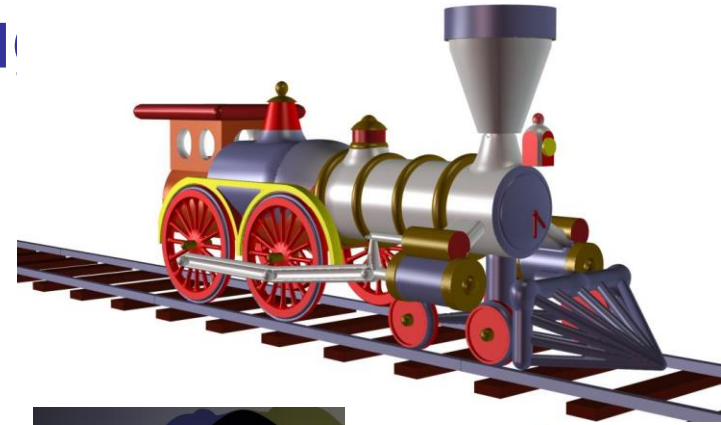
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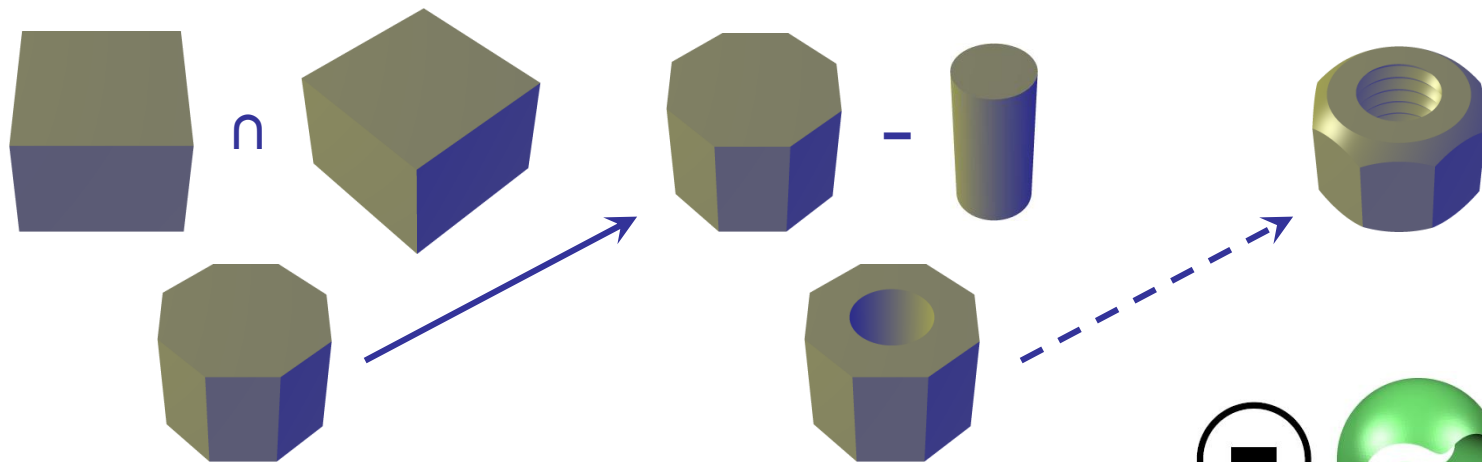
images courtesy of Brian Wyvill et al.



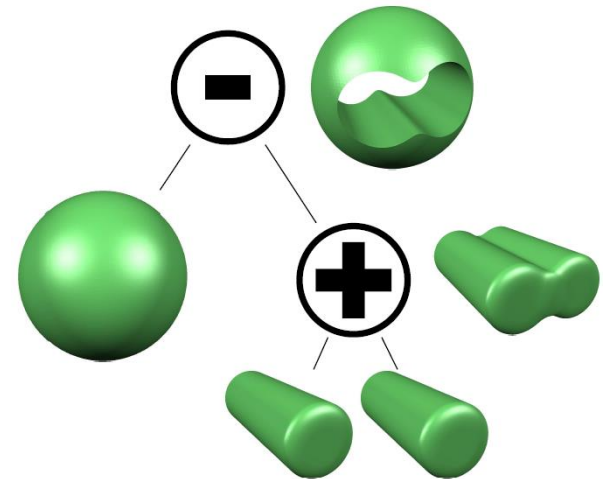
# Volumes: Construct. Solid Geometry

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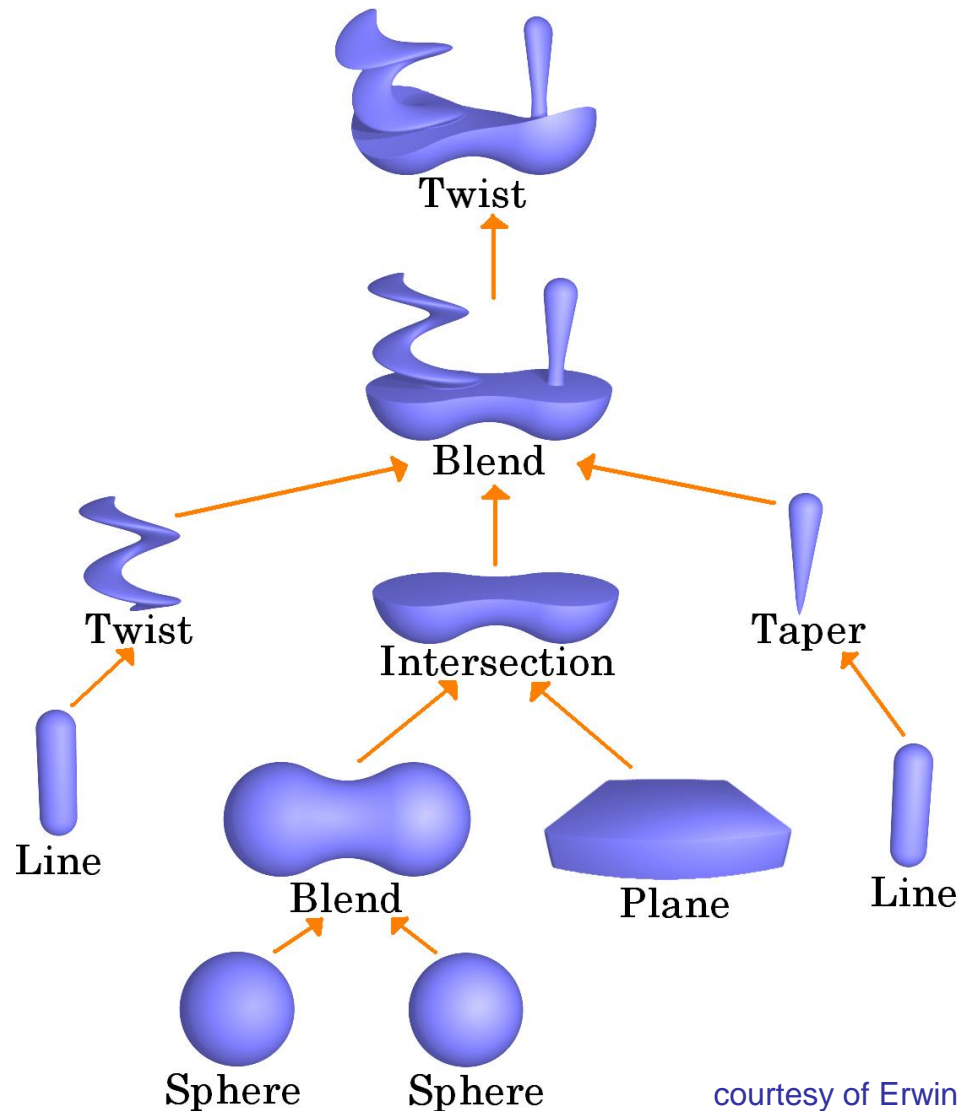
- Boolean operators to combine shapes
- unions, intersections, set differences



- build up CSG trees
- e.g., to build complex implicit models



# Implicit Surface CSG Trees: Blobtree

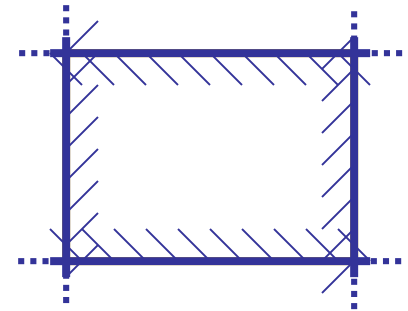


courtesy of Erwin de Groot and Brian Wyvill

# Volumes: BSP and Octrees

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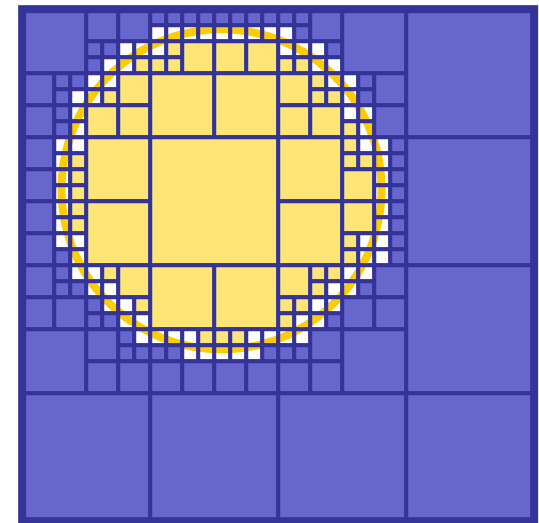
- space partitioning: define sub-spaces
- **binary space partitioning**: half-spaces
  - planes define borders between inside and outside; hierarchy
  - only current subspace affected



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- **binary space partitioning**: half-spaces
  - planes define borders between inside and outside; hierarchy
  - only current subspace affected
- **octrees**: partitioning on regular  $2 \times 2 \times 2$  grid (= 8)
  - mark cells inside, outside, or subdivide
  - 2D case: quadtrees ( $2 \times 2$ )



# Summary Object Representations

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- two types: boundary and volumetric representations
- we mostly use boundary representations
  - these store the surface of the objects
  - polygon/triangle-based or curve-based
  - flexible
- volumetric models also store the “inside”
- in addition to geometry we also store many other properties